

Problem Set 4

October 9, 2023

All numbered exercises are from the textbook *Calculus Vol. 3*, by OpenStax.

1. Exercises 3.3.103–111 (odd only).
2. Exercise 3.3.106.
3. Exercises 3.3.119–123 (odd only).
4. Exercise 3.3.130.
5. Exercises 3.3.131–139 (odd only).
6. Find an equation of a parabola that has curvature 4 at the origin.
7. At what point does the curve $y = \ln x$ have its maximum curvature? What happens to the curvature as $x \rightarrow \infty$?
8. Find the curvature of $\mathbf{r}(t) = \langle t, t^2, t^3 \rangle$ at the point $(1, 1, 1)$.
9. Let C be a smooth planar curve given by parametric equations $x = f(t)$, $y = g(t)$, where f and g are two times continuously differentiable functions. Show that the curvature of C is given by the formula

$$\kappa = \frac{|f'g'' - f''g'|}{[(f')^2 + (g')^2]^{3/2}}.$$

[Hint: Use the formula (3.16) from Theorem 3.6 in the text.]