Problem Set 3

January 28, 2024.

- **1.** Exercise 4.2 for Lebesgue measure in \mathbb{R}^n (with $n \in \mathbb{Z}_+$ arbitrary).
- **2.** Exercises 4.6–4.8.
- **3.** Exercises 4.13, 4.14.
- 4. (a) Show that every Vitali set $V \subset [0,1]$ has positive Lebesgue outer measure.
 - (b) Prove that for every $\epsilon > 0$, there exists a Vitali set V_{ϵ} satisfying $0 < m^*(V_{\epsilon}) < \epsilon$.
 - (c) Prove that for every Lebesgue measurable set $A \subset V$, we have m(A) = 0.

5. Exercise 4.17.