

**Problem Set 6**

March 3, 2024.

1. Exercise 7.25.
2. Exercise 8.5.
3. Exercise 8.7.
4. Exercise 9.4.
5. Exercise 11.3.
6. Exercise 11.6.
7. Exercises 11.8–11.11.
8. Let  $n \geq 2$  and let  $S$  be a standard  $n$ -simplex in  $\mathbb{R}^n$  with base of length  $a$ , for some  $a > 0$ . That is,

$$S := \{(x_1, \dots, x_n) \in \mathbb{R}^n : x_i \geq 0, \sum_{i=1}^n x_i \leq a\}.$$

Use Fubini Theorem (and induction) to find the Lebesgue integral  $\int_{\mathbb{R}^n} \chi_S$ .