

# Math 9412, Spectral Graph Theory

## Summer 2015

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(Presentation Topics)

List of topics for student presentations:

1. **Discrete Selberg trace formula.**  
Refs: Terras (Rep Theory of Finite Groups-last chapter); Forman (determinant of Laplacians on graphs).
2. **Electrical networks on graphs.**  
Kirchhoff's current and voltage laws, Kirchhoff's theorem for resistive networks, Thompson and Raleigh principles.  
Reference: *Random walks and electric networks* by Doyle and Snell. Sternberg, Vol 2.
3. **Perron-Frobenius theorem.**  
Reference: Many refs available, e.g. P. Lax's Linear Algebra.
4. **Vertex and edge Ihara zeta function of a graph. The determinant formula.**  
Reference: A. Terras
5. **The fundamental group and covering space of a graph. Galois theory for graphs.**  
Reference: A. Terras
6. **Spectra of Laplacians on finite symmetric spaces.**  
Ref. A. Terras.

7. **Ramanujan Graphs.**
8. **Kolmogorov complexity.**
9. **Shannon's channel coding theorem.**
10. **The trace formula for regular graphs: discrete path integral approach.**  
Reference: P. Mnev
11. **Plya's theorem for random walks in 1 and 2 dimensions.**  
References: many refs. available.
12. **Trace formula analysis of graphs.**  
Reference: B. Xiao, and R. Hancock.
13. **Coverings, heat kernels and spanning trees.**  
This is a very nice topic. 2 or 3 of you can team up and present the following paper: *Coverings, heat kernels and spanning trees*, by Chung and Yau.